

Arithmetic Sequences

Find the missing numbers

x	1	2	3	4	5	6	7	8
y	6.3	14.5	22.7		39.1	47.3		63.7
	$\overbrace{+8.2}^{\uparrow}$	$\overbrace{+8.2}^{\uparrow}$	$\overbrace{30.9}^{\uparrow}$			$\overbrace{55.5}^{\uparrow}$		

Arithmetic Sequence : a sequence of numbers that have a common difference between the terms

EX: Is this an arithmetic sequence?

$$\frac{1}{2}, \frac{1}{4}, 0, -\frac{1}{4}, -\frac{1}{2}$$
$$\overbrace{\frac{1}{4}}_{-\frac{1}{4}}, \overbrace{-\frac{1}{4}}_{-\frac{1}{4}}, \overbrace{-\frac{1}{4}}_{-\frac{1}{4}}$$

EX: $1, \underbrace{2, 4}_{+1, +2}, 8$

If we know the common difference, we can find the next term in the sequence

EX: 74, 67, 60, 53, $\frac{\uparrow}{46}$, $\frac{\uparrow}{39}$, $\frac{\uparrow}{32}$

EX: 9.5, 11, 12.5, $\frac{\uparrow}{14}$, $\frac{\uparrow}{15.5}$, $\frac{\uparrow}{17}$

1	2	3	4	
12	23	34	45	

without going one by one, how can I find the 100th term?

First Term 12

Second Term $12 + 11$

Third Term $12 + 11(2)$

Fourth Term $12 + 11(3)$

Fifth Term $12 + 11(4)$

100th Term $12 + 11(99)$

The nth term a_n of an arithmetic sequence with a first term a , and a common difference d is:

$$a_n = a_1 + \overset{\curvearrowleft}{(n-1)}d$$

Ex: $\underbrace{3, -10, -23, -36}_{-13} \quad$ Find the 15th term

$$d = -13 \quad a_1 = 3 \quad n = 15$$

$$\begin{aligned} a_{15} &= 3 + -13(15-1) \\ &= 3 + (-13)(15) + 13 \\ &= 3 - 195 + 13 \end{aligned}$$

$$a_{15} = -179$$

Ex: $\underbrace{23, 25, 27, 29}_{+2} \quad$ Find the 12th term

$$d = 2 \quad a_1 = 23 \quad n = 12$$

$$a_{12} = 23 + 2(12-1)$$

$$\frac{23 + 2(11)}{23 + 22} \quad a_{12} = 55$$